

6.4 Functions

Definition

Function: a relation between two values is classified as a function if each value within the domain corresponds to exactly one value in the range.

- You can test graphs through a Vertical Line Test. The line should only cross the graph at one point.

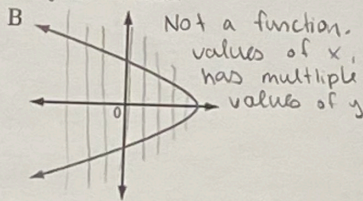
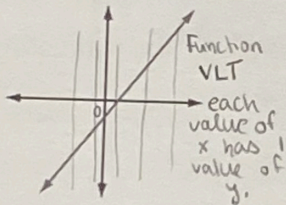
Function Notation

- a symbolic way of writing functions
- $f(c) \rightarrow f$ of c or f at c where f is your "y" representation and c is your "x" representation

Example 1 Determine Whether a Relation Is a Function

For each pair of relations, decide which relation is a function and which is not a function. Explain your choice.

a) A



b) C

x	y
2	5
2	7
4	9
6	11

Not a function when $x=2$, y can be either 5 or 7

D

x	y
-3	3
-2	4
-1	3
0	4

Function each value of x has only one value of y .

c) E $\{(1, 1), (2, 2), (3, 3), (4, 4)\} \times \{1\}$

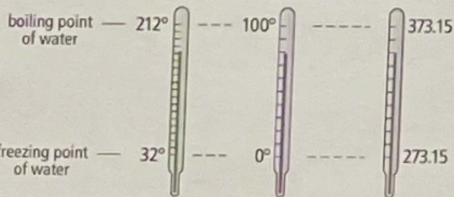
F $\{(1, 1), (1, 2), (1, 3), (1, 4)\}$

E Function. each value of x , has 1 value of y .

F Not a function. Each value of x has multiple values of y .

Example 2 Work With Function Notation

Fahrenheit Celsius Kelvin



The function $F(C) = 1.8C + 32$ is used to convert a temperature in degrees Celsius ($^{\circ}\text{C}$) to a temperature in degrees Fahrenheit ($^{\circ}\text{F}$).

a) Determine $F(25)$. Explain your answer.

b) Determine C so that $F(C) = 100$. Explain your answer.

a) $F(25)$ means $C=25$
 $F(25) = 1.8(25) + 32$
 $F(25) = 45 + 32$
 $F(25) = 77^{\circ}\text{F}$

b) $F(C) = 100$
 $100 = 1.8C + 32$
 $68 = 1.8C$
 $\frac{68}{1.8} = \frac{1.8C}{1.8}$
 $37.8\bar{C} = C$

Example 3 Graphing Linear Functions

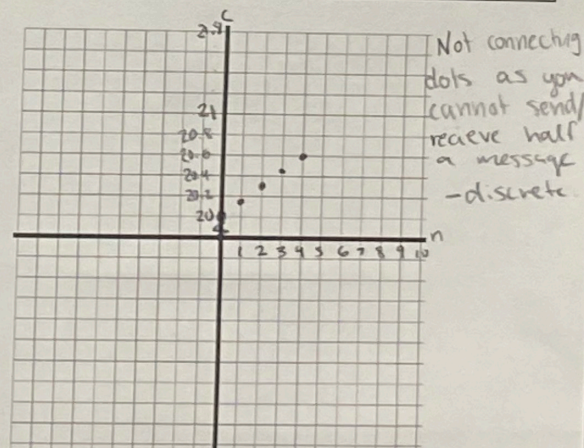
Skye has a cell phone plan for a monthly fee of \$20 plus 15c for each text message to or from a number not on a list of favourites. Skye's monthly bill can be modelled by the relation $C = 0.15n + 20$, where C is the total charge, in dollars, and n is the number of additional text messages.

- Write the relation in function notation.
- Make a table of values. Graph the function if Skye sends up to four additional text messages.
- If Skye's cell phone bill for a certain month is \$22.25, how many additional text message charges are there?

a) $C(n) = 0.15n + 20$

b)

n	0	1	2	3	4
Cost	20	20.15	20.30	20.45	20.60



c) 22.25

$C(n) = 0.15n + 20$

$C(n) = 22.25$

$22.25 = 0.15n + 20$

$2.25 = 0.15n$
 $\frac{2.25}{0.15} = \frac{0.15n}{0.15}$
 $15 = n$

she sent/received 15 messages.

